Using the operator method, solve the system of differential equations

$$
\begin{aligned}
& x^{\prime}-y=-e^{2 t} \\
& y^{\prime}-x=2 e^{2 t}
\end{aligned}
$$

Be sure to find the relationship among the coefficients in $x$ and $y$.

