Find the general solution $y = y_p + y_c$ to the following differential equation. Use the Euler-Cauchy method to find y_c and use the undetermined coefficients method to find y_p .

$$x^2 \frac{d^2 y}{dx^2} + x \frac{dy}{dx} + y = x + 1$$